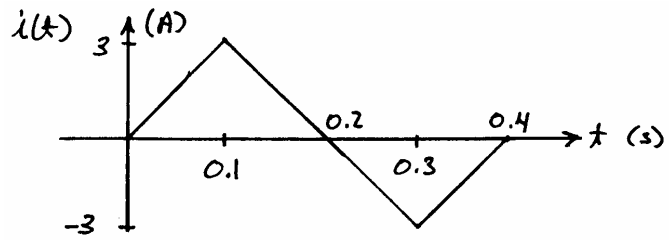
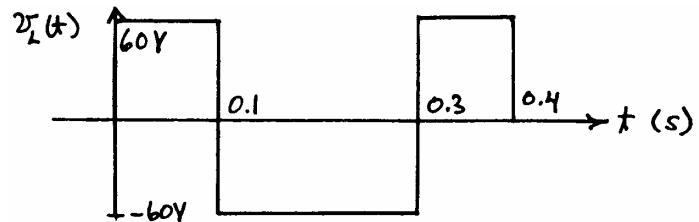


Homework # 5

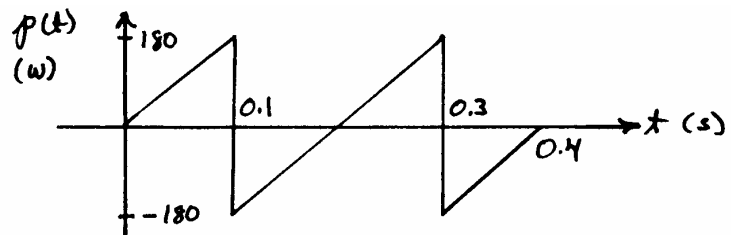
P3.40* $L = 2 \text{ H}$



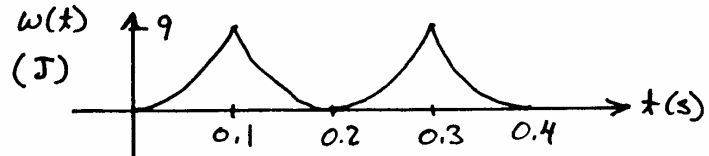
$$v_L(t) = L \frac{di_L(t)}{dt}$$



$$p(t) = v_L(t)i_L(t)$$



$$w(t) = \frac{1}{2} L [i_L(t)]^2$$



P3.45*

$$\begin{aligned} i_L(t) &= \frac{1}{L} \int_0^t v_L(t) dt + i_L(0) \\ &= 20 \times 10^3 \int_0^t 10 dt - 0.1 \\ &= 2 \times 10^5 t - 0.1 \text{ A} \end{aligned}$$

Solving for the time that the current reaches +100 mA, we have

$$i_L(t_x) = 0.1 = 2 \times 10^5 t_0 - 0.1$$

$$t_x = 1 \mu\text{s}$$

P3.46* $v_L = L \frac{di}{dt} = 0.5 \frac{4}{0.2} = 10 \text{ V}$

P3.53* (a) $L_{eq} = 1 + \frac{1}{1/2 + 1/(1+3)} = 2.333 \text{ H}$

(b) 2 H in parallel with 2 H is equivalent to 1H. Also, 2 H in parallel with 6 H is equivalent to 1.5 H. Finally, we have $L_{eq} = \frac{1}{1/4 + 1/(1+1.5)} = 1.538 \text{ H}$

P3.58* $i(t) = \frac{1}{L_{eq}} \int_0^t v(t) dt = \frac{L_1 + L_2}{L_1 L_2} \int_0^t v(t) dt$

$$i_1(t) = \frac{1}{L_1} \int_0^t v(t) dt$$

Thus, we can write $i_1(t) = \frac{L_2}{L_1 + L_2} i(t) = \frac{2}{3} i(t)$.

Similarly, we have $i_2(t) = \frac{L_1}{L_1 + L_2} i(t) = \frac{1}{3} i(t)$.

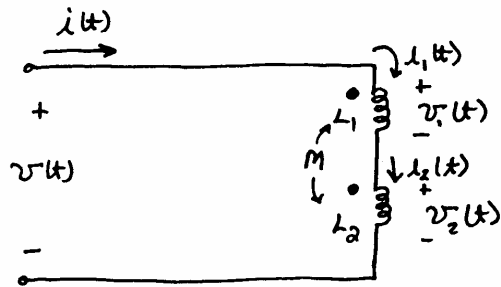
This is similar to the current-division principle for resistances. Keep in mind that these formulas assume that the initial currents are zero.

P3.63* With the dot moved to the bottom of L_2 , we have

$$v_1(t) = L_1 \frac{di_1(t)}{dt} - M \frac{di_2(t)}{dt} = 5 \cos(10t)$$

$$v_2(t) = -M \frac{di_1(t)}{dt} + L_2 \frac{di_2(t)}{dt} = 0$$

P3.64* (a)



As in Figure 3.23a, we can write

$$v_1(t) = L_1 \frac{di_1(t)}{dt} + M \frac{di_2(t)}{dt}$$

$$v_2(t) = M \frac{di_1(t)}{dt} + L_2 \frac{di_2(t)}{dt}$$

However, for the circuit at hand, we have $i(t) = i_1(t) = i_2(t)$.

Thus,

$$v_1(t) = (L_1 + M) \frac{di(t)}{dt}$$

$$v_2(t) = (L_2 + M) \frac{di(t)}{dt}$$

Also, we have $v(t) = v_1(t) + v_2(t)$.

Substituting, we obtain $v(t) = (L_1 + 2M + L_2) \frac{di(t)}{dt}$.

Thus, we can write $v(t) = L_{eq} \frac{di(t)}{dt}$, in which

$$L_{eq} = L_1 + 2M + L_2.$$

(b) Similarly, for the dot at the bottom end of L_2 , we have

$$L_{eq} = L_1 - 2M + L_2$$