

On Government Spending and Income Inequality under Monopolistic Competition*

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Abstract

This paper systematically examines the theoretical as well as quantitative interrelations between government spending and disposable-income inequality in a tractable monopolistically competitive Ramsey macroeconomy. Upon a higher government size, we analytically show that whether the long-run after-tax Gini coefficient rises or falls depends on the sign and magnitude of the wealth inequality effect versus those of the adjusted-labor effect. Under (i) a mild level of productive public expenditures and (ii) a sufficiently high intertemporal elasticity of consumption substitution, our calibrated model is able to generate qualitatively as well as quantitatively consistent income-inequality effects of government spending *vis-à-vis* recent estimation results.

Keywords: Government Spending; Income Inequality; Monopolistic Competition.

JEL Classification: D31, E30, H50.

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1 Introduction

The distributional impact of government spending on agents' disposable income has been an important research topic in the macroeconomics literature. Recently, Anderson et al. (2017) carry out a meta-regression analysis to synthesize empirical findings from 84 econometric studies with more than 900 estimates that have quantified the aggregate effects of various categories of public expenditures on several measures of post-tax income inequality. On the whole, these authors find a moderate and statistically significant inverse relationship between public spending and income inequality. Moreover, based on the panel data from multiple samples of OECD countries over the 1981 – 2005 period, Doerrenberg and Peichl (2014) report that a one-percent increase in the GDP share of total government purchases generates decreases in (i) the net-income Gini coefficient by 0.23% – 0.38% per fixed effects panel regressions; or (ii) an inequality measure estimated from the University of Texas Inequality Project (UTIP) data by 0.328% – 0.333% per the instrumental variable approach. Guzi and Kahanec (2018) also empirically investigate this subject with a panel data set from 30 advanced European economies for the time period of 2004 – 2015. Under two different sets of control variables, their fixed effects estimation yields that the resulting calculated elasticities of after-tax Gini with respect to government size (in absolute terms) are 0.22 and 0.26, respectively – these results turn out to be quantitatively consistent with Doerrenberg and Peichl's (2014, Table 1) earlier estimates.¹ In sum, the preceding pieces of work, together with numerous references therein, illustrate that there exists a discernible negative correlation between total government expenditure and after-tax income inequality, and that the estimated calculated elasticities range over the interval [0.22, 0.38].

Motivated by the aforementioned empirical evidence, this paper systematically examines the theoretical as well as quantitative interrelations between government spending and net-income inequality in a tractable monopolistically competitive macroeconomy with heterogeneous households in continuous time. In particular, we incorporate monopolistic competition and free entry/exit of intermediate goods-producing firms into a modified version of García-Peñalosa and Turnovsky's (2011) Ramsey model in which infinitely-lived agents merely differ in their initial capital endowments. Under the postulated homogenous and isoelastic preference formulation, the resultant macroeconomic equilibrium allocations are independent of wealth distribution, and will be identical to those within the corresponding representative-agent framework (Caselli and Ventura, 2000). This feature in turn allows us to analytically obtain the transitional dynamics and steady-state dispersions of capital/wealth and disposable

¹Using 2SLS estimations to account for the possible endogeneity of government size, Guzi and Kahanec (2018, Table 4) find that the corresponding calculated elasticity is raised to 0.98. However, these authors note that (in footnote 12) this estimated elasticity is not directly comparable to those based on OLS regressions.

income in terms of the economy's aggregate variables.

The production side of our macroeconomy consists of an intermediate-good segment whereby monopolistically competitive firms operate under pre-set constant overhead costs and a constant returns-to-scale Cobb-Douglas production function using capital and labor as inputs. Given the maintained assumption of free entry and exit, the equilibrium measure of these intermediate-input producers is endogenously determined through the zero-profit condition. This in turn generates increasing returns to product variety, *à la* Bénassy (1996) and Devereux et al. (1996), that will appear in the economy's social technology. A final output is then produced from the set of available differentiated intermediate goods in a perfectly competitive environment. For the baseline setting, public expenditures are postulated to be *useless* that do not contribute to firms' production or agents' utility functions. The government balances the budget at each instant of time by levying *only* lump-sum taxes on households to finance its purchases of final goods and services. These simplifications enable us to isolate how changes in the public-spending share affect the long-run distribution of after-tax income, as well as facilitate direct comparisons with the above-cited empirical studies in a focused and transparent manner. To provide a useful reference point for the subsequent quantitative results, numerical experiments are also conducted for our model economy under perfect competition, as in García-Peñalosa and Turnovsky (2011).

On the theoretical front, we analytically derive that at the model's steady state, the standard deviation of agents' disposable income is proportional to that of their relative capital stock by a positive scaling combo parameter which turns out to be a function of the public-spending share. We then show that in response to a change in the output proportion of government purchases, the long-run volatility of after-tax income may rise or fall depending on the directions as well as the strengths of two distinct effects. Start the economy from its original stationary macroeconomic allocations, together with an exogenously given initial distribution of capital endowments; and consider an increase in the GDP fraction of public expenditures that will generate the following outcomes. On the one hand, since a higher government size raises the steady-state aggregate capital stock, the macroeconomy undertakes an expansion in capital investment along the unique convergent equilibrium path toward the new long-run distribution of wealth measured in terms of relative capital stock. It can be shown that during the transition instants of time, capital-rich households will choose to work less and slow down their wealth accumulation rate; whereas capital-poor individuals will supply more hours worked and accumulate their wealth at a faster rate. As a result, the new stationary-state distribution of relative capital stock becomes less unequal than the initial counterpart – this is dubbed as *the wealth inequality effect* that is always negative. On the other hand, we find that the sign for the above-mentioned scaling combo parameter is theoretically indeterminate, which in

turn is determined by whether the economy-wide labor supply, adjusted by non-governmental expenditure share, increases or declines upon the occurrence of a larger public sector – this is dubbed as *the adjusted-labor effect*. In sum, our theoretical analysis demonstrates that when these two effects are of the same sign (opposite signs), the overall steady-state distributional consequence of an increase in government spending on households’ disposal income will be a definitely lower degree of inequality (analytically ambiguous).

Given the inconclusive nature of the preceding theoretical analysis, a quantitative assessment is undertaken to analyze the long-run income-inequality effects of government purchases within a calibrated version of our macroeconomy. In addition to assigning benchmark values to model parameters, different levels of market competitiveness are considered to numerically gauge the importance of imperfectly competitive product markets. We first find that the adjusted-labor effect is negative for each parametric configuration under consideration. This, together with the unambiguously negative wealth inequality effect, implies that a higher public-spending share will decrease the steady-state standard deviation of disposable income within the baseline setting. However, the associated calculated elasticity of after-tax Gini with respect to public expenditures under perfect competition ($= 0.0515$) is significantly lower than the estimated range of $0.22 - 0.38$ reported by Doerrenberg and Peichl (2014) and Guzi and Kahanec (2018). When the degree of monopoly market power rises, the economy’s speed of convergence toward the new stationary state will be slowed down, which in turn enhances the declining dispersion of agents’ relative capital distribution along the transition path. As a result, the wealth inequality effect becomes stronger; but the resulting calculated elasticities remain too low to be empirically realistic. In sum, it is shown that in the context of our benchmark Ramsey model, monopolistic competition *alone* does not lead to a quantitative match with the actual data on the long-run distributional consequences of government spending.

With regard to the sensitivity analysis, we find that since *ceteris paribus* an increase in the intertemporal-elasticity-of-substitution (IES) parameter strengthens the substitution effect of agents’ consumption expenditures across different instants of time, the accumulation rate of aggregate capital stock toward the new steady state upon a larger government size will be reduced. This in turn yields a stronger wealth inequality effect, whereas the magnitude of the corresponding (negative) adjusted-labor effect remains unaffected. It follows that the long-run standard deviations of relative capital stock and the after-tax income, as well as the Gini coefficient, will all fall further *vis-à-vis* those under the benchmark parameterization. Nevertheless, the ensuing calculated elasticities (ranging between 0.0661 and 0.1563) are still unrealistically low compared to recent estimation results.

In light of these numerical findings in the baseline framework, we examine an otherwise identical monopolistically competitive Ramsey model with *useful* government purchases of

goods and services. On the economy’s supply side, public spending may enter the representative final-output firm’s production technology as an externality that is complementary to intermediate inputs *à la* Barro (1990). On the economy’s demand side, government expenditure may enter the household utility nonseparably as a positive preference externality *à la* García-Peñalosa and Turnovsky (2011). While keeping other parameter values unchanged, incorporating productive government spending results in a higher percentage increase of the stationary-state aggregate capital stock as the public-expenditure share increases. This outcome will slow down the convergence speed of capital along the economy’s stable arm of the equilibrium saddle path, which in turn decreases the post-tax income dispersion because of a stronger wealth inequality effect. It turns out that under the logarithmically separable preference formulation in consumption and leisure (*i.e.* $IES = 1$), the perfectly competitive version of our model with a mild level of productive government purchases delivers a calculated elasticity ($= 0.222$) that is marginally above the lower bound of the estimated interval $[0.22, 0.38]$. When either the monopolistic market power or each agent’s intertemporal elasticity of consumption substitution rises, the resulting elasticities of after-tax Gini with respect to government spending will increase to $0.2301 - 0.3373$, which are a much closer fit with the empirical evidence.

We also find that under nonseparable utility-generating public expenditures, the long-run distribution of agents’ labor hours will become less unequal in response to a higher government size, regardless of whether private consumption and public goods are Edgeworth substitutes or complements. This in turn leads to a weaker wealth inequality effect because of the negative correlation between the dispersion of labor supply and that of relative capital stock during the transition. In this environment, the associated calculated elasticities will be lower than those in the benchmark model with wasteful government purchases, hence they are not empirically plausible either. Overall, this paper shows that our calibrated monopolistically competitive Ramsey model with (i) a mild level of productive public expenditures and (ii) a sufficiently high intertemporal elasticity of substitution in consumption is able to generate qualitatively as well as quantitatively consistent income-inequality effects of government spending *vis-à-vis* recent econometric studies as in Doerrenberg and Peichl (2014) and Guzi and Kahanec (2018).

The remainder of this paper is organized as follows. Section 2 describes our baseline Ramsey macroeconomy, discusses its equilibrium conditions and distributional dynamics, and then analytically derive the Gini coefficient associated with the long-run distribution of agents’ disposable income. Section 3 theoretically as well as quantitatively examines the income-inequality effects of government spending within the benchmark model. Section 4 studies an otherwise identical monopolistically competitive economy with productive or utility-generating public expenditures of final goods and services. Section 5 concludes.

2 The Economy

Our analysis begins with incorporating monopolistic competition and free entry/exit of intermediate goods-producing firms into a simplified version of García-Peñalosa and Turnovsky's (2011) Ramsey model with heterogeneous households in continuous time. Agents live forever, and derive utilities from consumption and leisure under a homogeneous and isoelastic preference formulation; and they only differ in terms of their initial capital endowments. On the production side of our macroeconomy, there is an intermediate-good segment in which monopolistically competitive firms operate with fixed set-up costs and a constant returns-to-scale Cobb-Douglas production technology using capital and labor as inputs. The equilibrium size and measure of these intermediate-input producers are endogenously pinned down by the zero-profit condition. A final output (GDP) is produced from the set of available differentiated intermediate goods in a perfectly competitive environment. The government balances the budget at each instant of time by levying lump-sum taxes on households to finance its purchases of final goods and services. For the sake of analytical simplicity, public expenditures are postulated to be useless that do not contribute to firms' production or agents' utility functions within our baseline setting. In addition, population growth, non-unitary elasticity of substitution between capital and labor in production, as well as other forms of taxation (*e.g.* capital, labor, or consumption) are not considered. These simplifications streamline our exposition that will enable us to examine the distributional effects of government spending under imperfect competition in a focused and transparent manner.

2.1 Firms

The production side of our model economy consists of two segments. As in Devereux et al. (1996, 2000), a single homogeneous final good Y_t is produced from a continuum of intermediate inputs x_{jt} with the following production technology:

$$Y_t = \left(\int_0^{N_t} x_{jt}^\rho dj \right)^{\frac{1}{\rho}}, \quad 0 < \rho < 1, \quad (1)$$

where N_t denotes the measure of (as well as the degree of variety for) intermediate goods utilized at time t , and ρ governs the elasticity of substitution between distinct intermediate inputs.² The final-good segment is postulated to be perfectly competitive, and we denote p_{jt} as the price of the j 'th intermediate good relative to the final output. The final goods-producing

²We have also examined Bénassy's (1996) formulation of the final-good production function given by $Y_t = N_t^{1+\omega-\frac{1}{\rho}} \left(\int_0^{N_t} x_{jt}^\rho dj \right)^{\frac{1}{\rho}}$, where $\omega > 0$ is a separate parameter that governs the level of product specialization. As it turns out, our quantitative results reported in sections 3.2 and 4 remain virtually unchanged with respect to this modification. Accordingly, our paper adopts a more parsimonious technological specification *à la* (1).

firms' profit maximization condition yields that

$$p_{jt} = \left(\frac{Y_t}{x_{jt}} \right)^{1-\rho}, \quad (2)$$

where the price elasticity of demand for x_{jt} is $\frac{1}{1-\rho}$; and the resulting markup ratio of price over marginal cost, given by $\frac{1}{\rho}$, characterizes the degree of market power for intermediate-good producers. In the limiting case of $\rho = 1$, all intermediate inputs are perfect substitutes for the production of Y_t , therefore the demand curve (2) will become perfectly elastic or horizontal.

Each intermediate good is produced by a monopolist with the Cobb-Douglas production specification in its own factor inputs:

$$x_{jt} = Ak_{jt}^a h_{jt}^b - Z, \quad A, a, b, Z > 0 \quad \text{and} \quad a + b = 1, \quad (3)$$

where A captures the technological state; k_{jt} and h_{jt} are capital and labor services employed by the j 'th intermediate-input firm; and Z represents a constant amount of intermediate goods that must be expended as fixed set-up costs before any production is undertaken. Since $a + b = 1$, the incidence of such overhead costs implies that the intermediate-good technology (3) exhibits increasing returns-to-scale. We also note that when $\rho = 1$ and $Z = 0$, the economy's production structure will collapse to one with only perfectly competitive final-goods producing firms, as studied by García-Peñalosa and Turnovsky (2011).

Using equations (2) and (3), together with the assumption that factor markets are perfectly competitive, it is straightforward to show that the first-order conditions for the j 'th intermediate-input producer's profit maximization problem are

$$r_t = \frac{\rho a (x_{jt} + Z) p_{jt}}{k_{jt}} \quad \text{and} \quad w_t = \frac{\rho b (x_{jt} + Z) p_{jt}}{h_{jt}}, \quad (4)$$

where r_t is the capital rental rate and w_t is the real wage rate. Under the maintained assumption of free entry and exit for intermediate goods-producing firms, their profit will be equal to zero at each instant of time. This zero-profit condition together with (4) yield the constant equilibrium quantity of intermediate input j :

$$x_{jt} = \frac{\rho Z}{1 - \rho} > 0, \quad (5)$$

which also represents the j 'th intermediate-good producer's size that turns out to be independent of any endogenous variable. In what follows, our analysis is restricted to the model's symmetric equilibrium in which

$$p_{jt} = p_t, \quad x_{jt} = x_t, \quad k_{jt} = \frac{K_t}{N_t}, \quad h_{jt} = \frac{H_t}{N_t}, \quad \text{for all } j \in [0, N_t], \quad (6)$$

where $K_t \left(= \int_0^{N_t} k_{jt} dj \right)$ and $H_t \left(= \int_0^{N_t} h_{jt} dj \right)$ denote the total capital stock and labor hours demanded or employed by intermediate-input firms. Using equations (3), (5) and (6), it can be shown that the equilibrium measure of intermediate-good producers is

$$N_t = \left[\frac{A(1-\rho)}{Z} \right] K_t^a H_t^b > 0. \quad (7)$$

Next, after substituting (6)-(7) into (1) and (3), we find that the economy's reduced-form production function is given by

$$Y_t = N_t^{\frac{1}{\rho}} x_t = \rho \left(\frac{1-\rho}{Z} \right)^{\frac{1-\rho}{\rho}} \left(AK_t^a H_t^b \right)^{\frac{1}{\rho}}, \quad (8)$$

where $\frac{a}{\rho} < 1$ to rule out the possibility of sustained endogenous growth, and $N_t^{\frac{1}{\rho}}$ represents a measure of aggregate productivity. Since the monopolistic-markup parameter ρ lies over the interval $(0, 1)$, the social technology (8) will exhibit increasing returns to an expansion in product variety N_t (Bénassy, 1996), which can be interpreted as endogenously enhancing the economy's total factor productivity. In addition, the level of aggregate returns-to-scale in production with respect to total capital and labor inputs is equal to $\frac{1}{\rho} > 1$.

Finally, plugging (6) and (8) into (2) shows that the symmetric-equilibrium price of each intermediate good is

$$p_t = N_t^{\frac{1-\rho}{\rho}}, \quad (9)$$

where N_t is given by (7). We can then combine equations (4)-(9) to derive that the symmetric-equilibrium factor prices are

$$r_t = a \frac{Y_t}{K_t}, \quad (10)$$

$$w_t = b \frac{Y_t}{H_t}, \quad (11)$$

hence the capital and labor shares of national income are equal to a and b , respectively.

2.2 Households

The economy is inhabited by a large number of infinitely-lived households whose population size is normalized to one for all t . These heterogeneous agents are indexed by i that is uniformly distributed over the interval $[0, 1]$. As in Turnovsky and García-Peñalosa (2008), individual i is endowed with one unit of labor hour at each instant of time and an initial level of capital stock K_{i0} ; and maximizes a discounted stream of utilities over its lifetime:

$$\int_0^{\infty} \underbrace{\frac{1}{\gamma} (C_{it} \ell_{it}^{\eta})^{\gamma}}_{\equiv U_{it}} e^{-\beta t} dt, \quad -\infty < \gamma < 1, \quad \eta, \beta > 0, \quad \text{and} \quad \gamma\eta < 1, \quad (12)$$

where C_{it} is consumption, ℓ_{it} is leisure, β is the subjective rate of time preference, $\frac{1}{1-\gamma}$ determines the intertemporal elasticity of substitution on “effective consumption” $C_{it} \ell_{it}^{\eta}$, and U_{it} is a homogenous utility function of degree $\gamma(1+\eta)$. Notice that when $\gamma = 0$, each household’s preference formulation becomes separable and logarithmic in both consumption and leisure, *i.e.* $U_{it} = \log C_{it} + \eta \log \ell_{it}$.

The budget constraint faced by individual i is given by

$$\dot{K}_{it} = r_t K_{it} + w_t H_{it} + \pi_{it} - C_{it} - T_{it} - \delta K_{it}, \quad K_{i0} > 0 \quad \text{given}, \quad (13)$$

where $H_{it} (= 1 - \ell_{it})$ denotes hours worked, π_{it} represents the profits as lump-sum dividends from agent i ’s ownership of intermediate-good firms, T_{it} denotes the lump-sum taxes collected by the government, and $\delta \in (0, 1)$ is the capital depreciation rate. The first-order conditions for this particular household’s dynamic optimization problem are

$$C_{it}^{\gamma-1} \ell_{it}^{\eta\gamma} = \lambda_{it}, \quad (14)$$

$$\eta \frac{C_{it}}{\ell_{it}} = w_t, \quad (15)$$

$$\frac{\dot{\lambda}_{it}}{\lambda_{it}} = \beta + \delta - r_t, \quad (16)$$

$$\lim_{t \rightarrow \infty} \lambda_{it} K_{it} e^{-\beta t} = 0, \quad (17)$$

where λ_{it} the co-state variable that characterizes the shadow (utility) value of physical capital. In addition, (15) equates the slope of individual i ’s indifference curve to the real wage, (16) is the consumption Euler equation and (17) is the transversality condition. After substituting (15) into (13), the capital accumulation equation for household i can be written as

$$\frac{\dot{K}_{it}}{K_{it}} = r_t - \delta + \left(1 - \frac{1+\eta}{\eta} \ell_{it}\right) \frac{w_t}{K_{it}} + \frac{\pi_{it} - T_{it}}{K_{it}}. \quad (18)$$

2.3 Government

The government spends its total (lump-sum) tax revenues T_t on goods and services produced by final-output producers, and maintains a balanced budget at each instant of time. Hence, its instantaneous budget constraint is given by

$$G_t = T_t = \int_0^1 T_{it} di, \quad (19)$$

where G_t is public expenditures that are postulated to be a constant fraction of the economy's aggregate output:

$$G_t = gY_t, \quad 0 < g < 1, \quad (20)$$

where Y_t is given by (8). Finally, combining the aggregated version of (13), together with $\pi_{it} = 0$ for all i and t , and (19) yields the following economy-wide resource constraint:

$$C_t + I_t + G_t = Y_t, \quad (21)$$

where C_t ($= \int_0^1 C_{it} di$) denotes total consumption spending, and I_t ($= \int_0^1 [\dot{K}_{it} + \delta K_{it}] di$) represents total gross investment.

2.4 Macroeconomic Equilibrium

This subsection derives the economy's equilibrium allocations expressed in terms of aggregate variables. We first take the time derivative on individual i 's marginal utility of consumption, given by (14), to obtain

$$(\gamma - 1) \frac{\dot{C}_{it}}{C_{it}} + \eta\gamma \frac{\dot{\ell}_{it}}{\ell_{it}} = \frac{\dot{\lambda}_{it}}{\lambda_{it}}, \quad (22)$$

which is equal to $\beta + \delta - r_t$ that is independent of i (see equation 16). This in turn implies that all agents choose the same growth rate for the shadow value of capital, regardless of how their capital endowments are initially distributed. We then take the time derivative on (15) which governs household i 's labor supply decision and follow Turnovsky and García-Peñalosa (2008, Appendix A.1) to find that

$$\frac{\dot{C}_{it}}{C_{it}} = \frac{\dot{C}_t}{C_t} \quad \text{and} \quad \frac{\dot{\ell}_{it}}{\ell_{it}} = \frac{\dot{\ell}_t}{\ell_t} \quad \text{for all } i \text{ and } t, \quad (23)$$

where ℓ_t ($= \int_0^1 \ell_{it} di$) denotes total leisure time. Equation (23) states that individual and aggregate quantities of consumption and leisure will grow at their respective common rates. In accordance with Caselli and Ventura (2000), the postulated homogenous and isoelastic preference formulation (12) results in macroeconomic equilibrium allocations that are independent of the wealth distribution within our model, and identical to those in the corresponding representative-agent setting which begins with an exogenously given K_0 ($= \int_0^1 K_{i0} di$). Moreover, the equalities of aggregate demand by intermediate goods-producing firms versus aggregate supply by heterogeneous households in the capital and labor markets are given by

$$\int_0^{N_t} k_{jt} dj = K_t = \int_0^1 K_{it} di, \quad (24)$$

$$\int_0^{N_t} h_{jt} dj = H_t = \int_0^1 H_{it} di. \quad (25)$$

Finally, taking aggregation over each household's first-order conditions as in (15) and (18), together with $\pi_t (= \int_0^1 \pi_{it} di) = 0$ and equations (8), (10)-(11), (19)-(20) and (24)-(25), yields that the economy-wide level of capital will accumulate over time according to

$$\frac{\dot{K}_t}{K_t} = \rho A^{\frac{1}{\rho}} \left(\frac{1-\rho}{Z} \right)^{\frac{1-\rho}{\rho}} \left[(1-g)H_t - \frac{b}{\eta}(1-H_t) \right] K_t^{\frac{a}{\rho}-1} H_t^{\frac{b}{\rho}-1} - \delta, \quad K_0 > 0 \text{ given.} \quad (26)$$

In addition, we use the aggregated version of condition (15), as well as equations (8), (11) and (22)-(25), to obtain the evolution of aggregate labor hours:

$$\frac{\dot{H}_t}{H_t} = \frac{\beta + \delta + \left[\frac{a(1-\gamma)}{\rho} \right] \frac{\dot{K}_t}{K_t} - \rho a A^{\frac{1}{\rho}} \left(\frac{1-\rho}{Z} \right)^{\frac{1-\rho}{\rho}} K_t^{\frac{a}{\rho}-1} H_t^{\frac{b}{\rho}}}{(1-\gamma) \left(1 - \frac{b}{\rho} \right) + [1-\gamma(1+\eta)] \left(\frac{H_t}{1-H_t} \right)}. \quad (27)$$

It follows that our baseline model's equilibrium conditions can be characterized by an autonomous pair of differential equations *à la* (26) and (27), which in turns implies that the dynamics of aggregate capital K_t and aggregate labor H_t are not affected by the initial wealth distribution.

2.5 Steady State

By setting $\dot{K}_t = \dot{H}_t = 0$ in (26) and (27), it is straightforward to show that our imperfectly competitive macroeconomy possesses a unique interior steady state given by

$$\tilde{H} = \frac{b(\beta + \delta)}{(\beta + \delta)[b + (1-g)\eta] - a\eta\delta}, \quad (28)$$

$$\tilde{K} = \left[A \left(\frac{1-\rho}{Z} \right)^{1-\rho} \left(\frac{\rho a}{\beta + \delta} \right)^{\rho} \tilde{H}^b \right]^{\frac{1}{\rho-a}}. \quad (29)$$

The remaining endogenous variables at the economy's stationary state can then be derived accordingly. Furthermore, under the empirically-realistic assumption that labor income accounts for a smaller percentage of GDP than households' aggregate consumption spending, the steady-state version of (26) leads to the following inequality:³

³At the model's stationary state, imposing $\dot{K}_t = 0$ on (26) yields that

$$\underbrace{(1-g)\tilde{Y} - \delta\tilde{K} - b\tilde{Y}}_{=\tilde{C}} = b \frac{\tilde{Y}}{\tilde{H}} \left[\frac{1}{\eta} - \left(\frac{1+\eta}{\eta} \right) \tilde{H} \right],$$

where \tilde{Y} and \tilde{C} are steady-state levels of total output and total consumption, respectively. Under the maintained assumption that $\frac{\tilde{C}}{\tilde{Y}} > b$, the left-hand-side of the above equation is strictly positive. It follows that the expression in the bracket on the right-hand-side must be positive as well, from which inequality (30) ensues.

$$\tilde{H} < \frac{1}{1 + \eta}, \quad (30)$$

which places an upper bound on the stationary economy-wide level of hours worked. From equation (28), it can then be shown that the effect on \tilde{H} of a permanent change in the output share of government purchases g is

$$\frac{\partial \tilde{H}}{\partial g} = \frac{b\eta(\beta + \delta)^2}{\{(\beta + \delta)[b + (1 - g)\eta] - a\eta\delta\}^2} > 0. \quad (31)$$

As is well known in the modern macroeconomics literature, a higher national income share of public spending (financed by additional lump-sum taxes on households) will raise the steady-state labor supply because of a negative wealth effect. However, this response is independent of the monopolistic-markup parameter ρ since it does not enter the expression for \tilde{H} . Since $\frac{\partial \tilde{K}}{\partial \tilde{H}} > 0$ per equation (29), we also note that the stationary level of aggregate capital stock becomes higher upon an increase in g .

2.6 Equilibrium Dynamics

In the neighborhood of the unique interior stationary state given by (28) and (29), our model's equilibrium conditions can be approximated by the linearized dynamical system:

$$\begin{bmatrix} \dot{K}_t \\ \dot{H}_t \end{bmatrix} = \underbrace{\begin{bmatrix} a_{11} & a_{12} \\ a_{21} & a_{22} \end{bmatrix}}_{\mathbf{J}} \begin{bmatrix} K_t - \tilde{K} \\ H_t - \tilde{H} \end{bmatrix}, \quad K_0 > 0 \text{ given}, \quad (32)$$

where \mathbf{J} is the Jacobian matrix of partial derivatives, and the analytical expressions for its elements are shown in Appendix. As in Turnovsky and García-Peñalosa (2008) and García-Peñalosa and Turnovsky (2011), our subsequent analysis will be restricted to environments in which the model's steady state is a locally determinate saddle point. Since the first-order dynamical system (26)-(27) possesses one predetermined variable K_t , the economy displays saddle-path stability and equilibrium uniqueness if and only if the two real eigenvalues of \mathbf{J} are of opposite signs with $Det(\mathbf{J}) = a_{11}a_{22} - a_{12}a_{21} < 0$. After some tedious but manageable algebra, we find that the requisite necessary and sufficient condition for local determinacy, expressed in terms of a lower bound on the monopolistic-markup parameter, is

$$\rho > \underbrace{\frac{b\eta(1 - \gamma)[(b - g)\delta + (1 - g)\beta]}{\eta(1 - \gamma)[(b - g)\delta + (1 - g)\beta] + b(\beta + \delta)[1 - \gamma(1 + \eta)]}}_{\equiv \rho_{\min}}, \quad (33)$$

under which the Jacobian's two eigenvalues are characterized by $\mu < 0 < \nu$. It follows that the stable branch of the economy's saddle path can be written as

$$K_t = \tilde{K} + (K_0 - \tilde{K})e^{\mu t}, \quad (34)$$

and

$$H_t = \tilde{H} + \frac{\mu - a_{11}}{a_{12}}(K_t - \tilde{K}), \quad (35)$$

where $a_{11} < 0$ and $a_{12} > 0$ per the proof in Appendix.

Intuitively, an increase in capital stock will reduce its growth rate because of diminishing marginal product of capital associated with the aggregate production function (8); thus $\frac{\partial \dot{K}_t}{\partial K_t} \Big|_{\dot{K}_t=0} = a_{11}$ is negative. In addition, a higher level of hours worked raises the rate of return to investment (see equation 10), which in turn will increase the accumulation rate of capital; thus $\frac{\partial \dot{K}_t}{\partial H_t} \Big|_{\dot{K}_t=0} = a_{12}$ is positive. On the other hand, the speed of convergence for the economy's equilibrium path toward the stationary state is determined by the modulus of μ , whose magnitude depends on model parameters in a rather complicated manner. It follows that the sign for the stable arm of the saddle point, given by $\frac{\mu - a_{11}}{a_{12}}$, is theoretically ambiguous. For all the empirically plausible parameterizations that are considered in sections 3.2 and 4, our model's stable locus (35) is negatively sloped; therefore labor hours are monotonically decreasing with respect to capital stock along the transition path.⁴ Given this relationship holds at each instant of time, we obtain that the initial labor relative to its steady-state level is governed by

$$H_0 - \tilde{H} = \underbrace{\frac{\mu - a_{11}}{a_{12}}}_{\text{Negative}}(K_0 - \tilde{K}). \quad (36)$$

Since K_0 is exogenously given and $\{\mu, a_{11}, a_{12}, \tilde{K}, \tilde{H}\}$ are functions of model parameters, equation (36) can be used to (endogenously) determine the unique value of H_0 that will place the economy on the convergent equilibrium trajectory.

2.7 After-Tax Income Inequality

This subsection analytically derives the economy's income inequality measured by the Gini coefficient based on the steady-state distribution of households' relative after-tax income. To this end, we follow García-Peñalosa and Turnovsky (2011) and postulate that the dynamic paths of individual and aggregate taxes-to-capital ratios are identical, *i.e.* $\frac{T_{it}}{K_{it}} = \frac{T_t}{K_t}$ for all i and t .⁵ Using the definition of $k_{it} \equiv \frac{K_{it}}{K_t}$ to denote agent i 's relative capital stock and $\pi_{it} = 0$

⁴This result turns out to be qualitatively equivalent to those in the perfectly-competitive settings of Turnovsky and García-Peñalosa (2008) and García-Peñalosa and Turnovsky (2011). Specifically, the stable locus in these authors' models is positively sloped: increasing leisure is associated with accumulating capital.

⁵We also find that the analytical as well as quantitative results, reported in section 3 below, remain qualitatively robust under an alternative distributional formulation for lump-sum taxes, $T_{it} = T_t$ for all i .

because of free entry/exit of intermediate-good firms, we combine equations (18) and (26) to derive that

$$\dot{k}_{it} = \frac{w_t}{K_t} \left\{ \left[\frac{(1+\eta)H_{it} - 1}{\eta} \right] - \left[\frac{(1+\eta)H_t - 1}{\eta} \right] k_{it} \right\}, \quad k_{i0} > 0 \text{ given.} \quad (37)$$

It follows that at the model's stationary state with $\dot{k}_{it} = 0$,

$$\tilde{H}_i - \tilde{H} = \left(\tilde{H} - \frac{1}{1+\eta} \right) \left(\tilde{k}_i - \underbrace{\tilde{k}}_{=1} \right) \quad (38)$$

holds for each household, where $\tilde{H} - \frac{1}{1+\eta} < 0$ per the inequality of (30) and $\tilde{k}_i \equiv \frac{\tilde{K}_i}{\tilde{K}}$. Since the response of hours worked to relative capital is common across all agents, the resulting aggregate labor supply will depend only on the economy-wide level of capital, but not on its distribution among heterogeneous households. In addition, equation (38) indicates that an agent with a higher relative capital stock will choose to work less and consume more leisure. This inverse relationship between wealth and labor hours turns out to be qualitatively consistent with the empirical evidence documented by Holtz-Eakin et al. (1993) and Algan et al. (2003), among others. Since $\frac{\dot{\ell}_{it}}{\ell_{it}} = \frac{\dot{\ell}_t}{\ell_t}$ (see equation 23) and $H_{it} + \ell_{it} = \ell_t + H_t = 1$ for all i and t , condition (38) also implies that

$$H_{it} = \phi_i H_t, \quad \text{where } \phi_i = \tilde{k}_i - \frac{\tilde{k}_i - 1}{(1+\eta)\tilde{H}} > 0 \text{ and } \int_0^1 \phi_i di = 1, \quad (39)$$

i.e. household i 's individual labor supply is a constant fraction of the economy's aggregate counterpart at each instant of time.

We then linearize the accumulation equation of relative capital stock (37) around the unique interior stationary state $\{\tilde{H}, \tilde{K}, \tilde{H}_i, \tilde{k}_i\}$ to find that⁶

$$\dot{k}_{it} = \frac{\tilde{w}}{\tilde{K}} \left\{ \frac{(1+\eta)(\phi_i - \tilde{k}_i)(H_t - \tilde{H})}{\eta} + \left[\frac{1 - (1+\eta)\tilde{H}}{\eta} \right] (k_{it} - \tilde{k}_i) \right\}, \quad (40)$$

where the steady-state real wage \tilde{w} is a function of \tilde{K} and \tilde{H} from (8) and (11). It is straightforward to show that the stable solution to the linearized differential equation (40) is given by

$$k_{it} = \tilde{k}_i + \frac{\tilde{w}}{(\alpha - \mu)\tilde{K}} \left(\frac{1+\eta}{\eta} \right) (\phi_i - \tilde{k}_i)(H_0 - \tilde{H})e^{\mu t}, \quad (41)$$

⁶The analytical expressions for \tilde{H} and \tilde{K} are given by equations (28)-(29). Given these aggregate quantities, we can use (38) and the steady-state version of (39) to solve for \tilde{H}_i and \tilde{k}_i .

where $\alpha \equiv \frac{b\beta(1+\eta)}{b(1+\eta)-g\eta} > 0$ and $\mu < 0$ is the stable eigenvalue associated with the model's Jacobian matrix as in (32).⁷ Substituting the expression of ϕ_i from (39) into (41), together with $\tilde{k} = 1$ and $H_t = H_0 e^{\mu t}$, results in the equilibrium time path of k_{it} :

$$k_{it} - 1 = \Omega_t (\tilde{k}_i - 1), \quad (42)$$

where

$$\Omega_t = 1 + \underbrace{\frac{\tilde{w}}{\eta(\alpha - \mu)\tilde{K}} \left(\frac{H_t}{\tilde{H}} - 1 \right)}_{\text{Positive}}. \quad (43)$$

Setting $t = 0$ in (42) yields that the standard deviation for the steady-state distribution of relative capital stock is given by⁸

$$\sigma_{\tilde{k}_i} = \frac{\sigma_{k_{i0}}}{\Omega_0}, \quad (44)$$

where the exogenously given $\sigma_{k_{i0}} > 0$ captures the dispersion of initial wealth distribution, and $\Omega_0 > 0$ represents the value of the volatility-adjustment coefficient (43) that governs the evolution of k_{it} at time 0.⁹

Next, we define the relative after-tax income of household i at time t as $y_{it}^a \equiv \frac{r_t K_{it} + w_t H_{it} - T_{it}}{r_t K_t + w_t H_t - T_t}$. Under the maintained assumption that $\frac{T_{it}}{K_{it}} = \frac{T_t}{K_t}$, in conjunction with the government's balanced budget constraint $G_t = T_t = gY_t$, it can be shown that the long-run volatility of agents' disposable income is¹⁰

⁷For the proof of $\alpha > 0$, we note that since $g\eta > 0$, $\frac{b\beta(1+\eta)}{b(1+\eta)-g\eta} > \frac{b\beta(1+\eta)}{b(1+\eta)} = \beta > 0$.

⁸After plugging $t = 0$ into (41), we obtain the stationary-state relative capital stock of agent i as follows:

$$\tilde{k}_i = \frac{k_{i0} + \frac{\tilde{w}}{\eta(\alpha-\mu)\tilde{K}} \left(\frac{H_0}{\tilde{H}} - 1 \right)}{1 + \frac{\tilde{w}}{\eta(\alpha-\mu)\tilde{K}} \left(\frac{H_0}{\tilde{H}} - 1 \right)}, \quad k_{i0} > 0 \text{ given,}$$

where $\{\alpha, \mu, \tilde{w}, H_0, \tilde{K}, \tilde{H}\}$ are functions of model parameters, and H_0 also depends on the initial (given) economy-wide capital stock K_0 (see equation 36). Using the $t = 0$ version of Ω_t as in (43), the preceding equation can be rewritten as $\tilde{k}_i = \frac{k_{i0} + \Omega_0 - 1}{\Omega_0}$, which in turn leads to equation (44) as well.

⁹Based on the last equation in footnote 8, the necessary and sufficient condition for $\tilde{k}_i > 0$ is given by $k_{i0} > \frac{1-\Omega_0}{\Omega_0}$. When the initial aggregate capital stock is lower than its steady-state level ($K_0 < \tilde{K}$), equation (36) yields that $H_0 > \tilde{H}$, which in turn implies that $\Omega_0 > 1$ from (43). Therefore, the requisite condition for a positive \tilde{k}_i always holds within this setting. When $K_0 > \tilde{K}$ and thus $H_0 < \tilde{H}$, it is straightforward to derive that $\Omega_0 < 1$, which will place a positive lower bound on k_{i0} . In this environment, $\Omega_0 > 0$ is further imposed to ensure that $\sigma_{\tilde{k}_i}$ in (44) is strictly positive. Furthermore, since $\sigma_{k_{it}} = \Omega_t \sigma_{\tilde{k}_i}$ per equation (42), our analysis will be restricted to the cases with $\Omega_t > 0$ for all $t > 0$.

¹⁰It is straightforward to find that the standard deviation of agent i 's relative before-tax income $y_{it} \equiv \frac{r_t K_{it} + w_t H_{it}}{r_t K_t + w_t H_t}$ at the model's steady state is given by $\sigma_{y_i} = \underbrace{\left[1 - \frac{b}{(1+\eta)\tilde{H}} \right]}_{\text{Positive}} \frac{\sigma_{k_{i0}}}{\Omega_0}$, which is *ceteris paribus*

higher than $\sigma_{\tilde{y}_i^a}$ for all values of $g \in (0, 1)$.

$$\sigma_{\tilde{y}_i^a} = \underbrace{\left[1 - \frac{b}{(1+\eta)(1-g)\tilde{H}} \right]}_{\equiv \Psi \in (0,1)} \underbrace{\frac{\sigma_{k_{i0}}}{\Omega_0}}_{= \sigma_{\tilde{k}_i}}. \quad (45)$$

In light of inequality $\tilde{H} < \frac{1}{1+\eta}$ given by (30), the term inside the right-hand-side bracket Ψ will be positive if $b+g < 1$ – this parametric restriction is empirically realistic as the sum of labor income and public spending does not exceed total output within U.S. and many developed countries. Since $\eta > 0$ and $0 < b, g, \tilde{H} < 1$, it is straightforward to obtain that $\Psi < 1$; thus equation (45) states that at the model’s stationary state, post-tax income is more equally distributed than relative capital stock ($\sigma_{\tilde{y}_i^a} < \sigma_{\tilde{k}_i}$). In addition, (44) and (45) together imply that the steady-state relative ranking on agents’ net income is identical to those of the long-run as well as the initial distributions of capital stock.

For the sake of analytical tractability, each household’s after-tax income is postulated to be randomly drawn from a log-normal distribution, as in Milanovic (2002), López and Servén (2006), Pinkovsky and Sala-i-Martin (2009) and Liberati (2015), among others. In this case, the resulting Gini coefficient (see Kleiber and Kotz, 2003, p. 117) that measures the economy’s after-tax income inequality is

$$Gini^a = 2 \underbrace{\int_0^{\frac{\sigma_{\tilde{y}_i^a}}{\sqrt{2}}} \frac{1}{\sqrt{2\pi}} e^{-\frac{u^2}{2}} du}_{= F\left(\frac{\sigma_{\tilde{y}_i^a}}{\sqrt{2}}\right)} - 1, \quad (46)$$

where $F(\cdot)$ stands for the c.d.f. of a standard normal distribution.

3 Government Spending and Income Inequality

This section examines the theoretical as well as quantitative interrelations between government spending and (after-tax) income inequality in our baseline macroeconomy with heterogeneous agents, endogenous entry and exit of intermediate goods-producing firms, and useless public expenditures. Since it is straightforward to show that $\sigma_{\tilde{y}_i^a}$ and $Gini^a$ are positively correlated as per equation (46), we first use (45) to analytically decompose changes in the steady-state volatility of agents’ disposable income into two distinct components. Next, we conduct a quantitative investigation on the distributional effects of changing the government size within a calibrated version of our imperfectly competitive model, and then confront the resulting numerical findings versus recent empirical estimates reported in Doerrenberg and Peichl (2014) and Guzi and Kahanec (2018), among others.

3.1 Theoretical Analysis

Using equation (45) and the chain rule, we find that the long-run income-volatility effect of government purchases on goods and services is given by

$$\frac{\partial \sigma_{\tilde{y}_i^a}}{\partial g} = \Psi \underbrace{\frac{\partial \sigma_{\tilde{k}_i}}{\partial g}}_{< 0} + \sigma_{\tilde{k}_i} \underbrace{\frac{\partial \Psi}{\partial g}}_{\geq 0}, \quad (47)$$

where

$$\frac{\partial \Psi}{\partial g} = \frac{a\eta\delta - b(\beta + \delta)}{(\beta + \delta)(1 + \eta)(1 - g)^2}. \quad (48)$$

Since $\beta, \delta, \eta > 0$ and $0 < g < 1$, it is immediately clear that

$$\frac{\partial \Psi}{\partial g} \geq 0 \text{ if and only if } a\eta\delta \geq b(\beta + \delta). \quad (49)$$

It follows that in response to a change in the output proportion of public spending, whether the resulting steady-state standard deviation of agents' after-tax income is larger or smaller than that at the initial instant of time depends on the signs as well as strength of the associated long-run impacts on (i) the variability of relative capital stock as captured by $\frac{\partial \sigma_{\tilde{k}_i}}{\partial g}$, and (ii) the aggregate labor hours adjusted by non-governmental expenditure share $(1 - g)\tilde{H}$ as governed by $\frac{\partial \Psi}{\partial g}$.

The underlying economic mechanism for the variability decomposition *à la* (47) can be understood as follows. Start our model from the original stationary allocations with $K_0 = \tilde{K}$ and $H_0 = \tilde{H}$ for the macroeconomy, as well as $k_{i0} = \tilde{k}_i$ for individual i ; and then consider an increase in the GDP fraction of government purchases that generates the ensuing outcomes. First, since a larger government size raises the steady-state quantity of aggregate capital stock to a higher level denoted as $\hat{K} > \tilde{K}$ (see equations 29 and 31), the economy undertakes an expansion in capital accumulation along the transition path that will monotonically converge toward the long-run distribution of wealth measured in terms of $\hat{k}_i \equiv \frac{\hat{K}_i}{\hat{K}}$. In this case under a new public-spending share g' , the beginning economy-wide amount of labor supply H'_0 is larger than that at the new stationary state given by \hat{H} (see equation 36), which in turn implies that the time-0 adjustment coefficient $\Omega_0 > 1$ per condition (43). It follows that as in (44), the resulting steady-state distribution of relative capital stock will be less unequal than the initial counterpart, *i.e.* $\sigma_{\hat{k}_i} < \sigma_{k_{i0}}$ – this is dubbed as *the wealth inequality effect*. Intuitively, after plugging the expression of ϕ_i from (39) into (41), we obtain that at $t = 0$:

$$\text{sgn}(k_{i0} - \hat{k}_i) = \text{sgn}[\underbrace{(\hat{k}_i - \tilde{k}_i)}_{= 1} \underbrace{(\hat{H} - H'_0)}_{\text{Negative}}]. \quad (50)$$

For agents who possess above the average level of aggregate wealth at the model's new steady state ($\hat{k}_i > \hat{k}$), the sign function of (50) shows that their relative capital stock will be decreasing on the convergent equilibrium trajectory with $k_{i0} > \hat{k}_i$. On the contrary, (50) also yields that the relative wealth of individuals who end up with $\hat{k}_i < \hat{k}$ will be increasing during the transition such that $k_{i0} < \hat{k}_i$ holds for these households. The aforementioned discussions altogether imply that the long-run distribution of wealth/capital will become less dispersed under a higher value of output share of public expenditures, hence $\frac{\partial \sigma_{\hat{k}_i}}{\partial g} < 0$.

Second, it is straightforward from the definition of Ψ as shown in (45) to find that

$$\text{sgn}\left(\frac{\partial \Psi}{\partial g}\right) = \text{sgn}\left(\frac{\partial[(1-g)\tilde{H}]}{\partial g}\right), \quad (51)$$

where $\frac{\partial \Psi}{\partial g}$ is given by (48) with an indeterminate sign. This theoretical ambiguity is caused by two opposing forces generated from an increase in the public-spending share: a decrease in $(1-g)$ versus a higher economy-wide level of hours worked in that $\frac{\partial \tilde{H}}{\partial g} > 0$ à la (31) – this is dubbed as *the adjusted-labor effect*. It follows that it is uncertain *a priori* whether the long-run “adjusted” aggregate labor supply will rise or fall when the corresponding wealth distribution becomes less unequal because of a higher g , *i.e.* $(1-g')\hat{H} \gtrless (1-g)\tilde{H}$.

In sum, this subsection finds that upon an increase in the output proportion of government spending, the wealth inequality effect always leads to a reduction in the long-run variability of relative capital stock, which in turn mitigates the extent of after-tax income inequality. Moreover, the adjusted-labor effect will further decrease $\sigma_{\tilde{y}_i^e}$ provided the necessary and sufficient condition for $\frac{\partial \Psi}{\partial g} < 0$, given by (49), is satisfied. When these two effects are of opposite signs with $\frac{\partial \sigma_{\hat{k}_i}}{\partial g} < 0$ and $\frac{\partial \Psi}{\partial g} > 0$, the overall steady-state distributional impact of public expenditures on households' disposal income is analytically ambiguous.

3.2 Quantitative Analysis

In light of the inconclusive nature of the above theoretical analysis, this subsection undertakes a quantitative assessment on the long-run income-inequality effects of public spending within a calibrated version of our baseline macroeconomy. Specifically, the model is postulated to start at a stationary state with $K_0 = \tilde{K}$, $H_0 = \tilde{H}$, and $k_{i0} = \tilde{k}_i$. For the benchmark parameterization, the capital and labor shares of national income, a and b , are 0.4 and 0.6, respectively; the subjective rate of time preference β is 0.04; the capital depreciation rate δ is 0.06; the technological state A and the fixed set-up costs Z under monopolistic competition are both normalized to 1; and the preference parameter η is set to be 2.2951 such that the initial steady-state level of aggregate labor hours is 0.3 according to (28). As in García-Peñalosa and Turnovsky (2011), the beginning government size g is chosen to be 0.15; and the intertemporal

elasticity of substitution (IES) associated with the household’s “effective consumption” *à la* (12) is selected to be 0.4, which in turn implies that $\gamma = -1.5$.

On the other hand, we note that $\frac{1}{\rho}$ is equal to the markup ratio of price over marginal cost with its empirical estimates ranging between 1 and 1.7; see Hall (1986), Domowitz et al. (1988), Morrison (1990) and Chirinko and Fazzari (1994), among others. It follows that the empirically plausible values of ρ take on the interval $[0.59, 1]$. Moreover, (8) shows that the level of aggregate returns-to-scale in production is also given by $\frac{1}{\rho}$. In this regard, Basu and Fernald (1997, Table 3) present a point estimate of 1.03 within the U.S. private business economy, after correcting reallocation of productive inputs across industries; whereas Laitner and Stolyarov (2004) report a preferred range of 1.09 – 1.11 for the U.S. economy. Based on these existing estimation results, the quantitative investigation below will explore parametric specifications with $\rho = 1$ (together with $Z = 0$), 0.97 and 0.9.

Our baseline measure of after-tax income inequality is calibrated to be the average Gini coefficient (based on disposable income, post taxes and transfers) of U.S., taken from OECD Income Distribution Database (2020), over the 2008-2017 period. Accordingly, $Gini^a$ is set to be 0.3876 at the economy’s original stationary state.¹¹ We then use equation (46) to obtain the corresponding magnitude of $\sigma_{\tilde{y}_i^a}$ ($= 0.7165$), with which the initial steady-state standard deviation of relative capital stock can be derived from (45), specifically $\sigma_{\tilde{k}_i} = 2.506$. Finally, under the maintained assumption that $k_{i0} = \tilde{k}_i$, condition (44) implies that the time-0 adjustment coefficient $\Omega_0 = 1$ for the benchmark calibration with $g = 0.15$.

3.2.1 Baseline Results

Given the above-mentioned benchmark values of model parameters, Table 1 presents the steady-state effects on selected key macroeconomic aggregates as well as the wealth and after-tax income inequalities of a one-percent permanent increase in the output share of public expenditures. Its “ $g = 0.15$ ” columns present the beginning levels of these variables, together with the corresponding values of Ω_0 and Ψ , at the model’s original steady state under various degrees of market competitiveness; whereas the “ $g' = 0.16$ ” columns report the resulting percentage changes relative to the initial counterparts. When $\rho = 1$ and $Z = 0$, the economy’s production structure collapses to García-Peñalosa and Turnovsky’s (2011) perfectly competitive formulation with a single representative output-producing firm. Hence, equation (7) becomes degenerate and we need to re-solve this special case from the scratch. As the monopolistic-markup parameter ρ decreases, our numerical simulations will *ceteris paribus*

¹¹We have also considered the initial value of $Gini^a = 0.3072$, which is the average after-tax Gini coefficient of 28 European countries between 2010 and 2018 as per Eurostat Database (2020). As it turns out, the results reported in Tables 1-4 below remain qualitatively and quantitatively robust to this alternative calibration.

help gauge the quantitative importance of imperfect competition on income inequality.¹² Since the distributional effects of government spending are influenced by the dynamics of aggregate variables, the top six rows of Table 1 will display these impacts first.

To understand the level effects shown in the upper portion of Table 1, we use the chain rule, combined with (8), (11) and (28)-(29), to find that the impact of a change in g on the steady-state real wage rate \tilde{w} is

$$\frac{\partial \tilde{w}}{\partial g} = \underbrace{\frac{(1 - \rho)\tilde{w}}{(\rho - a)\tilde{H}}}_{= \frac{\partial \tilde{w}}{\partial \tilde{H}}} \underbrace{\frac{\partial \tilde{H}}{\partial g}}_{\text{Positive}}, \quad (52)$$

where $a < \rho$ to ensure that our baseline model does not exhibit sustained endogenous growth *à la* (8), and $\frac{\partial \tilde{H}}{\partial g}$ is given by (31). It follows that $\frac{\partial \tilde{w}}{\partial g} > (=) 0$ when the markup ratio of price over marginal cost $\frac{1}{\rho} > (=) 1$. Intuitively, since the economy's social technology (8) displays constant returns-to-scale in K_t and H_t under the perfectly-competitive market structure ($\rho = 1$ and $Z = 0$), a higher labor supply shifting up the marginal product schedule for capital will increase investment and capital accumulation along the transition path. In the long run, there will be higher levels of aggregate capital and labor inputs, but the capital to labor ratio remains unchanged because of $a + b = 1$; see Baxter and King (1993, section III.B). It follows that capital, investment and aggregate output all rise by the same percentage as labor hours (= 1.161%) at the steady state. On the other hand, a constant long-run capital to labor ratio implies that the resulting relative factor price $\frac{\tilde{w}}{\tilde{r}}$ is fixed. Since the steady-state capital rental rate \tilde{r} ($= \beta + \delta$ from equation 16 with $\dot{\lambda}_{it} = 0$) is invariant to movements in g , the stationary level of real wage will not change either ($\frac{\partial \tilde{w}}{\partial g} = 0$).

In our monopolistically competitive specifications with $\rho \in (0, 1)$ and $Z = 1$, just like the aforementioned discussions under perfect competition, a larger government size raises the long-run labor hours, capital stock, gross investment and total output. This will also induce more entries of intermediate-goods producing firms as per equation (7). However, their quantitative results are quite different. For example, (8) shows that the economy with $\rho = 0.97$ exhibits a higher aggregate output elasticity with respect to hours worked than that with $\rho = 1$, which in turn generates an endogenous enhancement of the steady-state labor productivity $\frac{\tilde{Y}}{\tilde{H}}$. It follows from equation (11) that the real wage rate will rise (by 0.0612 percent) in the long run. In addition, given the parametric restriction of $a < \rho$, a higher stationary level of economy-wide labor supply (by 1.161 percent) leads to a more than proportional increase in the aggregate capital stock (by 1.2224 percent; see equation 29) and the measure of intermediate-input firms

¹²Since the numerical results do not change much when ρ falls further to below 0.9, Table 1 will not report these findings for the sake of space consideration.

(by 1.1852 percent). Finally, to maintain the constant capital rental rate at the steady state $\dot{a} = 0$ (10), total output will be increased by the same percentage as the capital stock in the long run.

In terms of the volatility/inequality responses reported in the bottom portion of Table 1, we first note that the benchmark parameterization of $\{a, b, \beta, \delta, \eta\}$ described above satisfies the requisite condition (49) for $\frac{\partial \Psi}{\partial g} < 0$. In particular, the scaling combo parameter Ψ falls by 0.0731 percent when the government size increases to $g' = 0.16$ within each parametric configuration under consideration. Per the decomposition equation (47), it follows that both the (unambiguously negative) wealth inequality effect as well as the adjusted-labor effect will decrease the steady-state standard deviation of agents' disposable income, hence an increase in government purchases leads to a lower degree of after-tax income inequality. However, the resulting long-run reduction in income inequality is quantitatively small. For the most parsimonious formulation with perfect competition ($\rho = 1$ and $Z = 0$), we find that a one-percent expansion in the public-spending share will yield a decrease in $Gini^a$ by 0.3434%, which in turn leads to a calculated elasticity (shown in the last row of Table 1) of 0.0515. This figure is significantly lower than the estimated range of 0.22 – 0.38 reported by Doerrenberg and Peichl (2014) and Guzi and Kahanec (2018).

With an imperfectly competitive production structure, Table 1 shows that the associated adjusted-labor effect (represented by $\frac{\Delta \Psi}{\Psi} = -0.0731\%$) is quantitatively independent of the calibrated values for ρ because it does not enter the expression of \tilde{H} or Ψ . Moreover, as discussed earlier, the percentage increase in the long-run aggregate capital stock gets bigger when the monopolistic-markup parameter ρ falls further. It follows that the economy's speed of convergence toward the new steady state will be slowed down, which in turn enhances the declining dispersion of agents' relative capital distribution along the transition path. As a result, the wealth inequality effect becomes stronger since the absolute value for the percentage reduction in $\sigma_{\tilde{k}_i}$ rises with a higher degree of monopoly market power. The preceding analysis thus implies that upon an increase in the government size within our benchmark parameterization, the decrease in after-tax income inequality or $Gini^a$ will be *ceteris paribus* larger under imperfect competition than that for the corresponding perfectly competitive formulation. Nevertheless, the resulting elasticities of after-tax Gini with respect to public expenditures (0.0523 when $\rho = 0.97$; and 0.0538 when $\rho = 0.9$) remain too low to be empirically realistic. In sum, we have found that in the context of our baseline macroeconomy, monopolistic competition *alone* does not help deliver a quantitative match with the actual data on the long-run distributional consequences of government spending.

3.2.2 Sensitivity Analysis

With regard to the sensitivity analysis, we find that the simulation results reported in Table 1 remain quantitatively robust to changes in $\{a, b, \beta, \delta, \eta, g\}$ over their respective empirically plausible ranges, as well as to different initial values of $\{Gini^a, \sigma_{\tilde{y}_i^a}, \sigma_{\tilde{k}_i}\}$. For each household's intertemporal elasticity of substitution ($IES = \frac{1}{1-\gamma}$), many previous studies have adopted the interval of $[\frac{1}{3}, 1]$ in their quantitative investigation; so does our baseline parameterization with $\gamma = -1.5$. However, some empirical research suggests that the elasticity of intertemporal consumption substitution is higher than one. For example, Vissing-Jørgensen and Attanasio (2003) report the point estimates of IES to be 1.03 (with six instruments) and 1.44 (under one instrumental variable) for the group of all stock holders. Gruber (2006) finds that the IES is around 2 when endogenous tax rate movements are included in his cross-sectional estimation on U.S. total non-durable consumption expenditures, and that this result is in line with Mulligan's (2002) earlier estimates based on time series data of total returns to capital. Drawing on these estimation findings, Table 2 presents numerical results of our model economy under alternative calibrations with $\gamma = -1$ ($IES = 0.5$); $\gamma = 0$ ($IES = 1$), hence the instantaneous utility function (12) is separable and logarithmic in consumption and leisure; and $\gamma = 0.4$ ($IES = 1.67$), which is close to its highest possible value that satisfies the requisite condition $\gamma\eta < 1$ for the preference concavity in leisure.

We note that since the steady-state expressions of aggregate labor hours \tilde{H} and capital stock \tilde{K} (see equations 28 and 29), as well as the remaining economy-wide variables $\{\tilde{w}, \tilde{I}, \tilde{Y}, \tilde{N}\}$, are independent of changes in agents' intertemporal elasticity of consumption substitution, the associated level effects from a higher public-spending share are quantitatively identical to those shown in the top six rows of Table 1. Accordingly, Table 2 will focus exclusively on the corresponding volatility/inequality responses. It turns out that the magnitude of the adjusted-labor effect remains unchanged, *i.e.* $\frac{\Delta\Psi}{\Psi} = -0.0731\%$, because variations of γ do not affect the scaling combo parameter Ψ given by (45). On the other hand, a higher γ or IES strengthens the intertemporal substitution effect of consumption across different instants of time, which in turn will reduce the accumulation rate of aggregate capital stock toward the new stationary state \hat{K} upon an expansion in g .¹³ We numerically verify this result by finding $\frac{\partial|\mu|}{\partial\gamma} < 0$, indicating that the stable eigenvalue's modulus becomes smaller as the IES rises. Table 2 thus shows that when the government size is increased to $g' = 0.16$ within each parametric specification, the resulting percentage increases of the time-0 volatility-adjustment coefficient, given by (43) with $\frac{\partial\Omega_0}{\partial|\mu|} < 0$, are *ceteris paribus* monotonically increasing with respect to γ . Using equations (44)-(46), it follows that the steady-state standard deviations of

¹³The same qualitative result can be obtained by incorporating convex adjustment costs into the law of motion for capital accumulation.

relative capital stock and after-tax income, as well as the Gini coefficient, will all fall further because of a stronger wealth inequality effect.¹⁴ Under $\rho = 0.9$ and $\gamma = 0.4$, these outcomes in turn raise the calculated elasticity to 0.1563 (shown in the last row of Table 2), which is still unrealistically low *vis-à-vis* estimation results of previous econometric studies.

4 Useful Government Spending

In the context of our baseline model studied above, government purchases are postulated to yield no substitution effects in that they do not influence the marginal conditions associated with the households' consumption/savings nor the firms' production decisions. However, the assumption of wasteful public spending, although commonly adopted in the academic literature for analytical simplicity, is not necessarily the most realistic – at least within U.S. and many developed countries. In this section, we will examine an identical monopolistically competitive macroeconomy, but with useful government expenditures on goods and services. On the economy's supply side, government spending may enter the representative final-good producer's production technology (1) as an externality that is complementary to intermediate inputs *à la* Barro (1990). On the economy's demand side, public expenditure may enter household i 's utility function (12) nonseparably as a positive preference externality *à la* García-Peñalosa and Turnovsky (2011). In what follows, numerical experiments are conducted to quantitatively assess the long-run distributional effects on agents' after-tax income under either productive or utility-generating government purchases within our model economy.

4.1 Productive Government Spending

In this case, a single homogeneous final output is produced by the following technology:

$$Y_t = \left(\int_0^{N_t} x_{jt}^\rho dj \right)^{\frac{1}{\rho}} G_t^\chi, \quad 0 < \rho < 1 \quad \text{and} \quad \chi > 0, \quad (53)$$

where χ captures the degree of positive external effects that government expenditures exert on the final-good firm's production process. Next, we follow the same solution procedure as in section 2 to find that (i) the economy's social technology now becomes

$$Y_t = \left[\rho A^{\frac{1}{\rho}} g^\chi \left(\frac{1-\rho}{Z} \right)^{\frac{1-\rho}{\rho}} K_t^{\frac{a}{\rho}} H_t^{\frac{b}{\rho}} \right]^{\frac{1}{1-\chi}}, \quad (54)$$

¹⁴García-Peñalosa and Turnovsky (2009) obtain the qualitatively identical result in a similar heterogeneous-household Ramsey model, but with fixed labor supply and a non-unitary elasticity of substitution between capital and labor inputs. These authors' Figure 1 shows that for a given level of the elasticity of substitution in production, an increase in agents' IES will raise the likelihood of declining wealth inequality as the economy accumulates capital.

where $\frac{a}{\rho(1-\chi)} < 1$ to eliminate the occurrence of persistent economic growth, and the resulting level of aggregate returns-to-scale in total capital and labor inputs is equal to $\frac{1}{\rho(1-\chi)}$, which is higher than that of (8) under useless public spending; (ii) the autonomous pair of differential equations that govern the dynamic trajectories of K_t and H_t are

$$\frac{\dot{K}_t}{K_t} = \left[\rho A^{\frac{1}{\rho}} g^\chi \left(\frac{1-\rho}{Z} \right)^{\frac{1-\rho}{\rho}} \right]^{\frac{1}{1-\chi}} \left[(1-g)H_t - \frac{b}{\eta}(1-H_t) \right] K_t^{\frac{a}{\rho(1-\chi)}-1} H_t^{\frac{b}{\rho(1-\chi)}-1} - \delta, \quad K_0 > 0 \quad \text{given,} \quad (55)$$

$$\frac{\dot{H}_t}{H_t} = \frac{\beta + \delta + \left[\frac{a(1-\gamma)}{\rho(1-\chi)} \right] \frac{\dot{K}_t}{K_t} - \frac{a}{K_t} \left[\rho A^{\frac{1}{\rho}} g^\chi \left(\frac{1-\rho}{Z} \right)^{\frac{1-\rho}{\rho}} K_t^{\frac{a}{\rho}} H_t^{\frac{b}{\rho}} \right]^{\frac{1}{1-\chi}}}{(1-\gamma) \left[1 - \frac{b}{\rho(1-\chi)} \right] + [1-\gamma(1+\eta)] \left(\frac{H_t}{1-H_t} \right)}; \quad (56)$$

and (iii) the necessary and sufficient condition for saddle-path stability is given by

$$\chi < 1 - \frac{b\eta(1-\gamma)[(b-g)\delta + (1-g)\beta]}{\underbrace{\rho \{ \eta(1-\gamma)[(b-g)\delta + (1-g)\beta] + b(\beta + \delta)[1-\gamma(1+\eta)] \}}_{\equiv \chi^{\max}}}. \quad (57)$$

Based on existing empirical estimates for the output elasticity of government spending that range from 0.03 (Eberts, 1986) to 0.39 (Aschauer, 1989), a “conservative” figure of $\chi = 0.1$ is adopted in our subsequent quantitative analyses. Table 3 presents the resulting volatility and inequality effects under identical calibrations of $\{a, b, \beta, \delta, \eta\}$ as in the benchmark model, together with the monopolistic-markup parameter $\rho = \{1, 0.97, 0.9\}$ and the household’s IES $\gamma = \{-1, 0, 0.4\}$, for ease of comparative comparisons with Table 2.¹⁵

We first note that since the scaling combo parameter Ψ defined in (45) is independent of χ , the magnitude of the adjusted-labor effect will remain unaffected (given by $\frac{\Delta\Psi}{\Psi} = -0.0731\%$) upon an expansion in the government size across Tables 2 and 3. In addition, while keeping the values of other parameters the same, the percentage changes reported in the remaining “ $g' = 0.16$ ” cells, as well as the calculated elasticities, of Table 3 under $\chi = 0.1$ are all larger (in absolute terms) than those corresponding to Table 2 with $\chi = 0$. Intuitively, although adding productive public expenditures does not affect the steady-state aggregate labor hours \tilde{H} per equation (28), the associated economy-wide level of capital stock is changed to

$$\tilde{K} = \left\{ A \left(\frac{1-\rho}{Z} \right)^{1-\rho} \left[\rho g^\chi \left(\frac{a}{\beta + \delta} \right)^{1-\chi} \right]^\rho \tilde{H}^b \right\}^{\frac{1}{\rho(1-\chi)-a}}. \quad (58)$$

¹⁵As in Table 1 with $\gamma = -1.5$ and $\chi = 0$, the calculated elasticities of after-tax income inequality with respect to public expenditures under $\gamma = -1.5$ and $\chi = 0.1$ remain too small to be empirically realistic. Hence, we choose not to report these results in Table 3 because of space consideration.

It follows that a higher g will raise the long-run total labor supply by the same proportion under either useless or productivity-augmenting government spending (see equation 31). However, a side-by-side comparison of (29) versus (58) yields that this equalized increase in \tilde{H} leads to a larger response of the stationary-state aggregate capital stock (in percentage term) when $\chi = 0.1$, because the relevant elasticity exponent $\frac{1}{\rho(1-\chi)-a} > \frac{1}{\rho-a}$ when $0 < \chi < 1 - \frac{a}{\rho}$ to rule out the possibility of sustained endogenous growth. This outcome decreases the capital accumulation rate that in turn will slow down the economy's convergence speed toward the new steady state (reflected by $\frac{\partial|\mu|}{\partial\chi} < 0$) along the stable arm of the equilibrium saddle path. As a result, the percentage increases in the time-0 volatility-adjustment coefficient Ω_0 shown in Table 3 are higher than those in the matching parameterizations of Table 2. This implies that as χ rises, the long-run distribution of relative capital stock will *ceteris paribus* become less unequal because of a stronger wealth inequality effect: the absolute value for the percentage reduction in $\sigma_{\tilde{k}_i}$ is monotonically increasing with the output elasticity of public expenditures. Consequently, the post-tax income inequality $\sigma_{\tilde{y}_i^a}$ and Gini coefficient $Gini^a$ are going to fall further as well.

In the context of a perfectly competitive macroeconomy ($\rho = 1$ and $Z = 0$), Table 3 shows that under the log-log utility function with $\gamma = 0$ and useful public spending with $\chi = 0.1$, a one-percent expansion of g will generate a decrease in $Gini^a$ by 1.4801%. This in turn leads to a calculated elasticity of 0.222, which is just slightly above the lower bound of the estimated interval [0.22, 0.38] that Doerrenberg and Peichl (2014) and Guzi and Kahanec (2018) have obtained. It follows that incorporating productive government expenditure alone into García-Peñalosa and Turnovsky's (2011) Ramsey model (without deviating from perfect competition) is able to deliver a rather marginal quantitative match with the actual data on the long-run distributional impact of government purchases. Moreover, as discussed in section 3, since an increase in the monopolistic market power (smaller ρ) or each household's intertemporal elasticity of consumption substitution (higher γ) strengthens the wealth inequality effect, the resulting elasticities of after-tax Gini with respect to public expenditures will be higher (0.2527 when $\rho = 0.9$ and $\gamma = 0$; 0.2884 when $\rho = 1$ and $\gamma = 0.4$; and 0.3373 when $\rho = 0.9$ and $\gamma = 0.4$), and thus provide a much closer fit with recent estimation results.

4.2 Utility-Generating Government Spending

In this case, household i 's discounted lifetime utilities are modified to

$$\int_0^\infty \frac{1}{\gamma} \underbrace{\left(C_{it}^\eta G_{it}^\theta \right)^\gamma}_{\equiv U_{it}} e^{-\beta t} dt, \quad -\infty < \gamma < 1, \quad \eta, \theta, \beta > 0, \quad \text{and} \quad \gamma\eta < 1, \quad (59)$$

where θ represents the degree of a positive preference externality that government spending exerts on the composite good $C_{it}\ell_{it}^\eta G_t^\theta$. When $\gamma = 0$, the time- t utility function U_{it} exhibits additive separability between private consumption, leisure and public good, hence the marginal utilities of C_t and ℓ_t are independent of G_t . When $\gamma > (<) 0$, the marginal utility of private consumption increases (decreases) with respect to government purchases, thus C_t and G_t are Edgeworth complements (substitutes).

It is then straightforward to derive that (i) all the first-order conditions that characterize firms' production decisions and factor demands, as shown in section 2.1, will remain unaffected; (ii) the steady-state quantities of aggregate labor hours and capital stock, given by (28)-(29), are independent of the preference-externality parameter θ ; and (iii) the autonomous pair of differential equations that determine the dynamic evolutions of K_t and H_t are equation (26) and

$$\frac{\dot{H}_t}{H_t} = \frac{\beta + \delta + \left[\frac{a(1-\gamma-\theta\gamma)}{\rho} \right] \frac{\dot{K}_t}{K_t} - \rho a A^{\frac{1}{\rho}} \left(\frac{1-\rho}{Z} \right)^{\frac{1-\rho}{\rho}} K_t^{\frac{a}{\rho}-1} H_t^{\frac{b}{\rho}}}{\frac{b\theta\gamma}{\rho} + (1-\gamma)(1-\frac{b}{\rho}) + [1-\gamma(1+\eta)] \left(\frac{H_t}{1-H_t} \right)}. \quad (60)$$

We also find that given $\theta > 0$, this economy's unique interior steady state always displays local determinacy over the interval $\gamma \in [0, 1)$, and that the necessary and sufficient condition for saddle-path stability with $\gamma < 0$ is

$$\theta < \frac{(\rho - b)(1 - \frac{1}{\gamma})[(b - g)\delta + (1 - g)\beta] + \frac{\rho b(\beta + \delta)}{\eta}(1 + \eta - \frac{1}{\gamma})}{\underbrace{b[(b - g)\delta + (1 - g)\beta]}_{\equiv \theta^{\max}}}. \quad (61)$$

Using García-Peñalosa and Turnovsky's (2011) calibration of $\theta = 0.3$, Table 4 presents the associated volatility and inequality effects under the same selected values of $\{a, b, \beta, \delta, \eta\}$ per the baseline parameterization, in conjunction with $\rho = \{1, 0.97, 0.9\}$ and $\gamma = \{-1, 0, 0.4\}$. We first note that as the preference formulation (59) become logarithmically separable in private consumption and public good ($\gamma = 0$), the inclusion of utility-enhancing government purchases does not have any impact on the model's equilibrium conditions and distributional dynamics. It follows that the numerical results reported in Tables 2 and 4 are identical when the household's IES is equal to 1. On the other hand, since θ does not enter the expression for the scaling combo parameter Ψ , the resulting size of the adjusted-labor effect remains unchanged upon an increase in the public-spending share within Tables 2 and 4.

Table 4 also shows that when $\gamma = -1$, the percentage reductions in the steady-state standard deviations of relative capital stock and post-tax income, as well as the Gini coefficient, are all smaller (in absolute terms) under $\theta = 0.3$ than those corresponding to Table 2 with $\theta = 0$. In this environment with C_t and G_t as Edgeworth substitutes, a higher g leads to

decreases in the marginal utilities of private consumption and leisure, which in turn induces each agent to work harder along the transition path such that the long-run distribution of individual hours worked will become less unequal. Using equations (38)-(39), it can be derived that there exists a negative correlation between the dispersion of labor supply and that of wealth¹⁶ because relatively poor (wealthy) households choose to accumulate their capital more rapidly (slowly) during the transition. Consequently, the resulting wealth inequality effect is weakened upon an increase in the government size. The same intuitive explanation is applicable to the setting with $\gamma = 0.4$, as the stationary-state volatility of labor hours will decline as well when private consumption and public good are preference complements. Thanks to a weaker wealth inequality effect, the calculated elasticities of *Gini*^a with respect to public spending under either non-separable specification of utility-generating government expenditure ($\gamma \neq 0$), as shown in the top and bottom portions of Table 4, are lower than those in Table 2 for the benchmark model. It follows that these numerical elasticity results are not empirically plausible compared to recent estimates found by Doerrenberg and Peichl (2014) and Guzi and Kahanec (2018). Overall, this paper shows that under (i) a mild level of productive public expenditures ($\chi = 0.1$) and (ii) a sufficiently high intertemporal elasticity of consumption substitution ($\gamma \geq 0$), our calibrated monopolistically competitive Ramsey model is able to generate qualitatively as well as quantitatively realistic income-inequality effects of government spending *vis-à-vis* previous econometric studies.

5 Conclusion

Recent empirical studies have documented that there exists a discernible negative correlation between aggregate public expenditures and net-income inequality, and that the estimated calculated elasticities of after-tax Gini with respect to government size range over the interval [0.22, 0.38]. Motivated by these stylized facts, this paper examines the distributional impact of government spending on agents' disposable income, not only theoretically but also quantitatively, in a tractable monopolistically competitive Ramsey model with heterogeneous households and free entry/exit of intermediate goods-producing firms. We analytically show that upon an increase in the GDP fraction of government purchases, whether the long-run income distribution becomes more or less unequal is governed by the direction and size of the (unambiguously negative) wealth inequality effect versus those of the (ambiguously indeterminate) adjusted-labor effect. In a calibrated version of the model economy, our baseline setting correctly yields that a higher wasteful public-spending share will decrease the steady-state dis-

¹⁶This result is qualitatively consistent with that in equation (21) of Turnovsky and García-Peñalosa (2008, p. 1411) under perfect competition and useless government spending. Specifically, the steady-state volatilities of agents' leisure and relative capital stock are positively correlated.

persion of post-tax income, but the resulting calculated elasticities as shown in Tables 1 and 2 are too low to be empirically realistic. In light of these numerical findings, an otherwise identical monopolistically competitive Ramsey macroeconomy with useful government purchases of final goods and services is analyzed. We find that under (i) a mild level of productive public expenditures and (ii) a sufficiently high intertemporal elasticity of substitution in consumption, our augmented model is able to generate qualitatively as well as quantitatively consistent income-inequality effects of government spending *vis-à-vis* the estimation results reported by Doerrenberg and Peichl (2014) and Guzi and Kahanec (2018).

This paper can be extended in several directions. In particular, it would be worthwhile to incorporate specific categories of government expenditures that have been found to exert statistically significant effects on income inequality into our Ramsey model, such as social security and welfare, education, and public health, among others. Moreover, while this paper focuses exclusively on the spending side of government budget, it would also be valuable to examine the distributional consequences of distortionary income taxation. These possible extensions will enhance our understanding of how distinct types of government purchases and/or different fiscal policy rules affect income inequality within a monopolistic competitive macroeconomy. We plan to pursue these research projects in the near future.

6 Appendix

It can be shown that the elements which make up the benchmark model's Jacobian matrix \mathbf{J} as shown in (32) are

$$a_{11} = \underbrace{\rho A^{\frac{1}{\rho}} \left(\frac{1-\rho}{Z} \right)^{\frac{1-\rho}{\rho}}}_{\text{Positive}} \left(\frac{a}{\rho} - 1 \right) \left[(1-g)\tilde{H} - \frac{b}{\eta}(1-\tilde{H}) \right] \underbrace{\tilde{K}^{\frac{a}{\rho}-1} \tilde{H}^{\frac{b}{\rho}-1}}_{\text{Positive}}, \quad (\text{A.1})$$

$$a_{12} = \underbrace{\rho b A^{\frac{1}{\rho}} \left(\frac{1-\rho}{Z} \right)^{\frac{1-\rho}{\rho}}}_{\text{Positive}} \left\{ \frac{1}{\rho} \left[(1-g)\tilde{H} - \frac{b}{\eta}(1-\tilde{H}) \right] + \frac{1}{\eta} \right\} \underbrace{\tilde{K}^{\frac{a}{\rho}} \tilde{H}^{\frac{b}{\rho}-2}}_{\text{Positive}}, \quad (\text{A.2})$$

$$a_{21} = \frac{\rho a A^{\frac{1}{\rho}} \left(\frac{1-\rho}{Z} \right)^{\frac{1-\rho}{\rho}} \left(\frac{a}{\rho} - 1 \right) \left\{ \left[\frac{(1-\gamma)(1-g)}{\rho} - 1 \right] \tilde{H} - \frac{b(1-\gamma)}{\rho\eta}(1-\tilde{H}) \right\} \tilde{K}^{\frac{a}{\rho}-2} \tilde{H}^{\frac{b}{\rho}}}{(1-\gamma)\left(1-\frac{b}{\rho}\right) + [1-\gamma(1+\eta)] \left(\frac{\tilde{H}}{1-\tilde{H}} \right)}, \quad (\text{A.3})$$

$$a_{22} = \frac{\rho a A^{\frac{1}{\rho}} \left(\frac{1-\rho}{Z} \right)^{\frac{1-\rho}{\rho}} \left\{ \frac{b}{\rho} \left[\frac{(1-\gamma)(1-g)}{\rho} - 1 \right] \tilde{H} - \frac{b(1-\gamma)}{\rho\eta} \left[\frac{b(1-\tilde{H})}{\rho} - 1 \right] \right\} \tilde{K}^{\frac{a}{\rho}-1} \tilde{H}^{\frac{b}{\rho}-1}}{(1-\gamma)\left(1-\frac{b}{\rho}\right) + [1-\gamma(1+\eta)] \left(\frac{\tilde{H}}{1-\tilde{H}} \right)}, \quad (\text{A.4})$$

where \tilde{H} and \tilde{K} are given by (28) and (29).

Using the steady-state version of the aggregate capital accumulation equation (26) with $\dot{K}_t = 0$, it is straightforward to show that

$$(1 - g)\tilde{H} - \frac{b}{\eta}(1 - \tilde{H}) = \frac{\delta}{\rho A^{\frac{1}{\rho}} \left(\frac{1-\rho}{Z}\right)^{\frac{1-\rho}{\rho}} \tilde{K}^{\frac{a}{\rho}-1} \tilde{H}^{\frac{b}{\rho}-1}} > 0, \quad (\text{A.5})$$

which, combined with $\frac{a}{\rho} < 1$ to rule out sustained long-run economic growth, leads to $a_{11} < 0$. In addition, condition (A.5) together with $\eta > 0$ and $\rho \in (0, 1)$ imply that $a_{12} > 0$.

References

- [1] Algan, Y., A. Cheron, J.-O. Hairault and F. Langot (2003), “Wealth Effect on Labor Market Transitions,” *Review of Economic Dynamics* 6, 156-178.
- [2] Anderson, E., M.A.J. D’Orey, M. Duvendack, and L. Esposito (2017), “Does Government Spending Affect Income Inequality? A Meta-Regression Analysis,” *Journal of Economic Surveys* 31, 961-987.
- [3] Aschauer, D.A. (1989), “Is Public Expenditure Productive?” *Journal of Monetary Economics* 23, 177-200.
- [4] Barro, R.J. (1990), “Government Spending in a Simple Model of Endogenous Growth,” *Journal of Political Economy* 98, S103-S125.
- [5] Basu, S., and J.G. Fernald (1997), “Returns to Scale in U.S. Production: Estimates and Implications,” *Journal of Political Economy* 105, 249-283.
- [6] Baxter, M. and R.G. King (1993), “Fiscal Policy in General Equilibrium,” *American Economic Review* 83, 315-334.
- [7] Bénassy, J.-P. (1996), “Monopolistic Competition, Increasing Returns to Specialization and Output Persistence,” *Economic Letters* 52, 187-191.
- [8] Caselli, F. and J. Ventura (2000), “A Representative Consumer Theory of Distribution,” *American Economic Review* 90, 909-926.
- [9] Chirinko, R. and S. Fazzari (1994), “Economic Fluctuations, Market Power, and Returns to Scale: Evidence from Firm-Level Data,” *Journal of Applied Econometrics* 9, 47-70.
- [10] Devereux, M.B., A.C. Head and B.J. Lapham (1996), “Monopolistic Competition, Increasing Returns, and the Effects of Government Spending,” *Journal of Money, Credit and Banking* 28, 233-254.
- [11] Devereux, M.B., A.C. Head and B.J. Lapham (2000), “Government Spending and Welfare with Returns to Specialization,” *Scandinavian Journal of Economics* 102, 547-561.
- [12] Domowitz, I., G. Hubbard and B. Petersen (1988), “Market Structure and Cyclical Fluctuations in U.S. Manufacturing,” *Review of Economics and Statistics* 70, 55-66.
- [13] Doerrenberg, P. and A. Peichl (2014), “The Impact of Redistributive Policies on Inequality in OECD Countries,” *Applied Economics* 17, 2066-2086.
- [14] Eberts, R.W. (1986), “Estimating the Contribution of Urban Public Infrastructure to Regional Growth,” Federal Reserve Bank of Cleveland, Working Paper No. 8610.
- [15] Eurostat Database (2020), <https://ec.europa.eu/eurostat>.
- [16] García-Peñalosa, C. and S.J. Turnovsky (2009), “The Dynamics of Wealth Inequality on A Simple Ramsey Model: A Note on the Role of Production Flexibility,” *Macroeconomic Dynamics* 13, 250-262.
- [17] García-Peñalosa, C. and S.J. Turnovsky (2011), “Taxation and Income Distribution Dynamics in a Neoclassical Growth Model,” *Journal of Money, Credit and Banking* 43, 1543-1577.
- [18] Gruber, J. (2006), “A Tax-Based Estimate of the Elasticity of Intertemporal Substitution,” National Bureau of Economic Research, Working Paper 11945.

- [19] Guzi, M. and M. Kahanec (2018), “Income Inequality and the Size of Government: A Causal Analysis,” IZA Institute of Labor Economics, Discussion Paper No. 12015.
- [20] Hall, R. (1986), “Market Structure and Macroeconomic Fluctuations,” *Brookings Papers on Economic Activity* 2, 285-338.
- [21] Holtz-Eakin, D., D. Joulfaian and H.S. Rosen (1993), “The Carnegie Conjecture: Some Empirical Evidence,” *Quarterly Journal of Economics* 108, 413-435.
- [22] Kleiber, C. and S. Kotz (2003), *Statistical Size Distributions in Economics and Actuarial Sciences*, Hoboken, New Jersey: John Wiley & Sons.
- [23] Laitner, J. and D. Stolyarov (2004), “Aggregate Returns to Scale and Embodied Technical Change: Theory and Measurement using Stock Market Data,” *Journal of Monetary Economics* 51, 191-233.
- [24] Liberati, P. (2015), “The World Distribution of Income and Its Inequality, 1970-2009,” *Review of Income and Wealth* 61, 248-273.
- [25] López, J.H. and L. Servén (2006), “A Normal Relationship? Poverty, Growth and Inequality,” World Bank, Policy Research Working Paper Series No. 3814.
- [26] Milanovic, B. (2002), “True World Income Distribution, 1988 and 1993: First Calculation Based on Household Surveys Alone,” *Economic Journal* 112, 51-92.
- [27] Morrison, C. (1990), “Market Power, Economic Profitability and Productivity Growth Measurement: An Integrated Structural Approach,” National Bureau of Economic Research, Working Paper 3355.
- [28] Mulligan, C. (2002), “Capital, Interest, and Aggregate Intertemporal Substitution,” National Bureau of Economic Research, Working Paper 9373.
- [29] OECD Income Distribution Database (2020): Gini, Poverty, Income, Methods and Concepts, <https://www.oecd.org/social/income-distribution-database.htm>.
- [30] Pinkovsky, M. and X. Sala-i-Martin (2009), “Parametric Estimations of the World Distribution of Income,” National Bureau of Economic Research, Working Paper 15433.
- [31] Turnovsky, S.J. and C. García-Peñalosa (2008), “Distributional Dynamics in a Neoclassical Growth Model: The Role of Elastic Labor Supply,” *Journal of Economic Dynamics and Control* 32, 1399-1461.
- [32] Vissing-Jørgensen, A. and O.P. Attanasio (2003), “Stock-Market Participation, Intertemporal Substitution, and Risk-Aversion” *American Economic Review Papers and Proceedings* 93, 383-391.

Table 1. Benchmark Model with Useless Government Spending and $\gamma = -1.5$

	$\rho = 1$ and $Z = 0$		$\rho = 0.97$ and $Z = 1$		$\rho = 0.9$ and $Z = 1$	
	$g = 0.15$	$g' = 0.16$	$g = 0.15$	$g' = 0.16$	$g = 0.15$	$g' = 0.16$
\tilde{w}	1.5117	no change	1.1762	0.0612%	0.7462	0.2312%
\tilde{H}	0.3	1.161%	0.3	1.161%	0.3	1.161%
\tilde{K}	3.0233	1.161%	2.3523	1.2224%	1.4924	1.3946%
\tilde{I}	0.1814	1.161%	0.1411	1.2224%	0.0895	1.3946%
\tilde{Y}	0.7558	1.161%	0.5881	1.2224%	0.3731	1.3946%
\tilde{N}	n.a.	n.a.	0.0205	1.1852%	0.057	1.2543%
$\sigma_{\tilde{k}_i}$	2.506	-0.3013%	2.506	-0.3069%	2.506	-0.3176%
$\sigma_{\tilde{y}_i^a}$	0.7165	-0.374%	0.7165	-0.3798%	0.7165	-0.3906%
$Gini^a$	0.3876	-0.3434%	0.3876	-0.3486%	0.3876	-0.3586%
Ω_0	1	0.302%	1	0.308%	1	0.319%
Ψ	0.2859	-0.0731%	0.2859	-0.0731%	0.2859	-0.0731%
$\left \frac{\Delta Gini^a / Gini^a}{\Delta g / g} \right $	0.0515		0.0523		0.0538	

Table 2. Benchmark Model with Useless Government Spending: Sensitivity Analysis under $\gamma = \{-1, 0, 0.4\}$

	$\rho = 1$ and $Z = 0$		$\rho = 0.97$ and $Z = 1$		$\rho = 0.9$ and $Z = 1$	
$\gamma = -1$	$g = 0.15$	$g' = 0.16$	$g = 0.15$	$g' = 0.16$	$g = 0.15$	$g' = 0.16$
$\sigma_{\tilde{k}_i}$	2.506	-0.4074%	2.506	-0.4218%	2.506	-0.4593%
$\sigma_{\tilde{y}_i^a}$	0.7165	-0.4801%	0.7165	-0.4948%	0.7165	-0.532%
$Gini^a$	0.3876	-0.4407%	0.3876	-0.4541%	0.3876	-0.4884%
Ω_0	1	0.409%	1	0.424%	1	0.461%
Ψ	0.2859	-0.0731%	0.2859	-0.0731%	0.2859	-0.0731%
$\left \frac{\Delta Gini^a / Gini^a}{\Delta g / g} \right $	0.0661		0.0681		0.0733	
$\gamma = 0$	$g = 0.15$	$g' = 0.16$	$g = 0.15$	$g' = 0.16$	$g = 0.15$	$g' = 0.16$
$\sigma_{\tilde{k}_i}$	2.506	-0.6792%	2.506	-0.7131%	2.506	-0.8073%
$\sigma_{\tilde{y}_i^a}$	0.7165	-0.7518%	0.7165	-0.7858%	0.7165	-0.8798%
$Gini^a$	0.3876	-0.6904%	0.3876	-0.7216%	0.3876	-0.808%
Ω_0	1	0.684%	1	0.718%	1	0.814%
Ψ	0.2859	-0.0731%	0.2859	-0.0731%	0.2859	-0.0731%
$\left \frac{\Delta Gini^a / Gini^a}{\Delta g / g} \right $	0.1036		0.1082		0.1212	
$\gamma = 0.4$	$g = 0.15$	$g' = 0.16$	$g = 0.15$	$g' = 0.16$	$g = 0.15$	$g' = 0.16$
$\sigma_{\tilde{k}_i}$	2.506	-0.8807%	2.506	-0.9282%	2.506	-1.0619%
$\sigma_{\tilde{y}_i^a}$	0.7165	-0.9531%	0.7165	-1.0004%	0.7165	-1.1342%
$Gini^a$	0.3876	-0.8754%	0.3876	-0.919%	0.3876	-1.0421%
Ω_0	1	0.888%	1	0.937%	1	1.073%
Ψ	0.2859	-0.0731%	0.2859	-0.0731%	0.2859	-0.0731%
$\left \frac{\Delta Gini^a / Gini^a}{\Delta g / g} \right $	0.1313		0.1378		0.1563	

Table 3. Productive Government Spending with $\chi = 0.1$ and $\gamma = \{-1, 0, 0.4\}$

	$\rho = 1, Z = 0$ and $\chi = 0.1$		$\rho = 0.97, Z = 1$ and $\chi = 0.1$		$\rho = 0.9, Z = 1$ and $\chi = 0.1$	
$\gamma = -1$	$g = 0.15$	$g' = 0.16$	$g = 0.15$	$g' = 0.16$	$g = 0.15$	$g' = 0.16$
$\sigma_{\tilde{k}_i}$	2.506	-0.8779%	2.506	-0.8943%	2.506	-0.9338%
$\sigma_{\tilde{y}_i^a}$	0.7165	-0.9502%	0.7165	-0.9668%	0.7165	-1.0061%
$Gini^a$	0.3876	-0.8728%	0.3876	-0.888%	0.3876	-0.9241%
Ω_0	1	0.886%	1	0.902%	1	0.942%
Ψ	0.2859	-0.0731%	0.2859	-0.0731%	0.2859	-0.0731%
$\left \frac{\Delta Gini^a / Gini^a}{\Delta g / g} \right $	0.1309		0.1332		0.1386	
$\gamma = 0$	$g = 0.15$	$g' = 0.16$	$g = 0.15$	$g' = 0.16$	$g = 0.15$	$g' = 0.16$
$\sigma_{\tilde{k}_i}$	2.506	-1.5383%	2.506	-1.5966%	2.506	-1.7606%
$\sigma_{\tilde{y}_i^a}$	0.7165	-1.6102%	0.7165	-1.6686%	0.7165	-1.8325%
$Gini^a$	0.3876	-1.4801%	0.3876	-1.5341%	0.3876	-1.685%
Ω_0	1	1.562%	1	1.623%	1	1.792%
Ψ	0.2859	-0.0731%	0.2859	-0.0731%	0.2859	-0.0731%
$\left \frac{\Delta Gini^a / Gini^a}{\Delta g / g} \right $	0.222		0.2301		0.2527	
$\gamma = 0.4$	$g = 0.15$	$g' = 0.16$	$g = 0.15$	$g' = 0.16$	$g = 0.15$	$g' = 0.16$
$\sigma_{\tilde{k}_i}$	2.506	-2.0188%	2.506	-2.1074%	2.506	-2.3723%
$\sigma_{\tilde{y}_i^a}$	0.7165	-2.0904%	0.7165	-2.179%	0.7165	-2.4436%
$Gini^a$	0.3876	-1.9226%	0.3876	-2.0044%	0.3876	-2.2487%
Ω_0	1	2.06%	1	2.153%	1	2.43%
Ψ	0.2859	-0.0731%	0.2859	-0.0731%	0.2859	-0.0731%
$\left \frac{\Delta Gini^a / Gini^a}{\Delta g / g} \right $	0.2884		0.3007		0.3373	

Table 4. Utility-Generating Government Spending with $\theta = 0.3$ and $\gamma = \{-1, 0, 0.4\}$

	$\rho = 1, Z = 0$ and $\theta = 0.3$		$\rho = 0.97, Z = 1$ and $\theta = 0.3$		$\rho = 0.9, Z = 1$ and $\theta = 0.3$	
$\gamma = -1$	$g = 0.15$	$g' = 0.16$	$g = 0.15$	$g' = 0.16$	$g = 0.15$	$g' = 0.16$
$\sigma_{\tilde{k}_i}$	2.506	-0.3663%	2.506	-0.3759%	2.506	-0.3979%
$\sigma_{\tilde{y}_i^a}$	0.7165	-0.4389%	0.7165	-0.4486%	0.7165	-0.4708%
$Gini^a$	0.3876	-0.403%	0.3876	-0.4118%	0.3876	-0.4321%
Ω_0	1	0.367%	1	0.377%	1	0.4%
Ψ	0.2859	-0.0731%	0.2859	-0.0731%	0.2859	-0.0731%
$\frac{ \Delta Gini^a / Gini^a }{\Delta g / g}$	0.0604		0.0618		0.0648	
$\gamma = 0$	$g = 0.15$	$g' = 0.16$	$g = 0.15$	$g' = 0.16$	$g = 0.15$	$g' = 0.16$
$\sigma_{\tilde{k}_i}$	2.506	-0.6792%	2.506	-0.7131%	2.506	-0.8073%
$\sigma_{\tilde{y}_i^a}$	0.7165	-0.7528%	0.7165	-0.7858%	0.7165	-0.8798%
$Gini^a$	0.3876	-0.6904%	0.3876	-0.7216%	0.3876	-0.808%
Ω_0	1	0.684%	1	0.718%	1	0.814%
Ψ	0.2859	-0.0731%	0.2859	-0.0731%	0.2859	-0.0731%
$\frac{ \Delta Gini^a / Gini^a }{\Delta g / g}$	0.1036		0.1082		0.1212	
$\gamma = 0.4$	$g = 0.15$	$g' = 0.16$	$g = 0.15$	$g' = 0.16$	$g = 0.15$	$g' = 0.16$
$\sigma_{\tilde{k}_i}$	2.506	-0.8683%	2.506	-0.9138%	2.506	-1.0407%
$\sigma_{\tilde{y}_i^a}$	0.7165	-0.9407%	0.7165	-0.986%	0.7165	-1.113%
$Gini^a$	0.3876	-0.864%	0.3876	-0.9056%	0.3876	-1.0224%
Ω_0	1	0.876%	1	0.922%	1	1.052%
Ψ	0.2859	-0.0731%	0.2859	-0.0731%	0.2859	-0.0731%
$\frac{ \Delta Gini^a / Gini^a }{\Delta g / g}$	0.1296		0.1358		0.1534	